

Imperfections – deformation and microstructures in polycrystals

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7- On the hexagonal-close-packed crystal structure

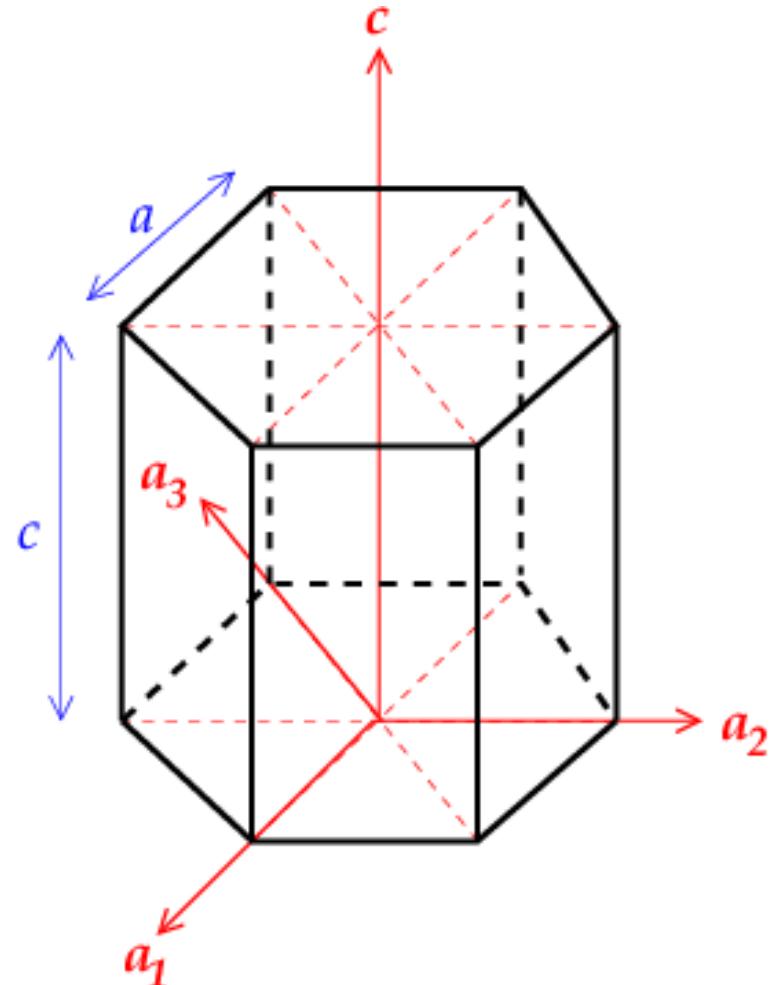
Hexagonal-close-packed (hcp)

Metals with an hcp structure:

- Zirconium, titanium, magnesium, zinc, ϵ -iron ($P > 15$ GPa)

Interest :

- Zirconium alloys(zircalloy) in nuclear industry (fuel rods in nuclear reactors)
- Titanium alloys: airplane engines
- Magnesium: car industry (lighter than steel)
- ϵ -iron: geophysics, Earth's inner core



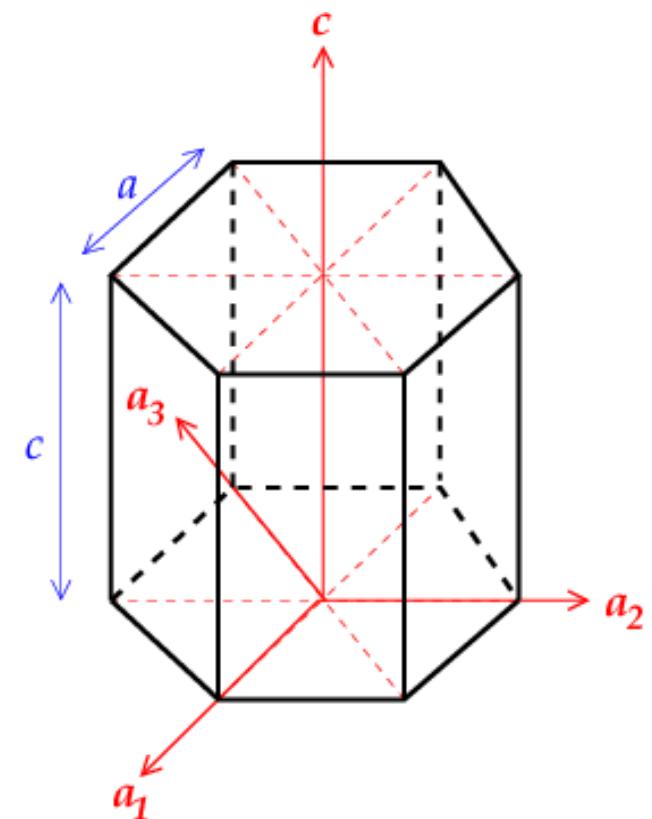
4 indices notation

Vectors a_1 , a_2 and a_3 are equivalent and non-orthogonal to each other

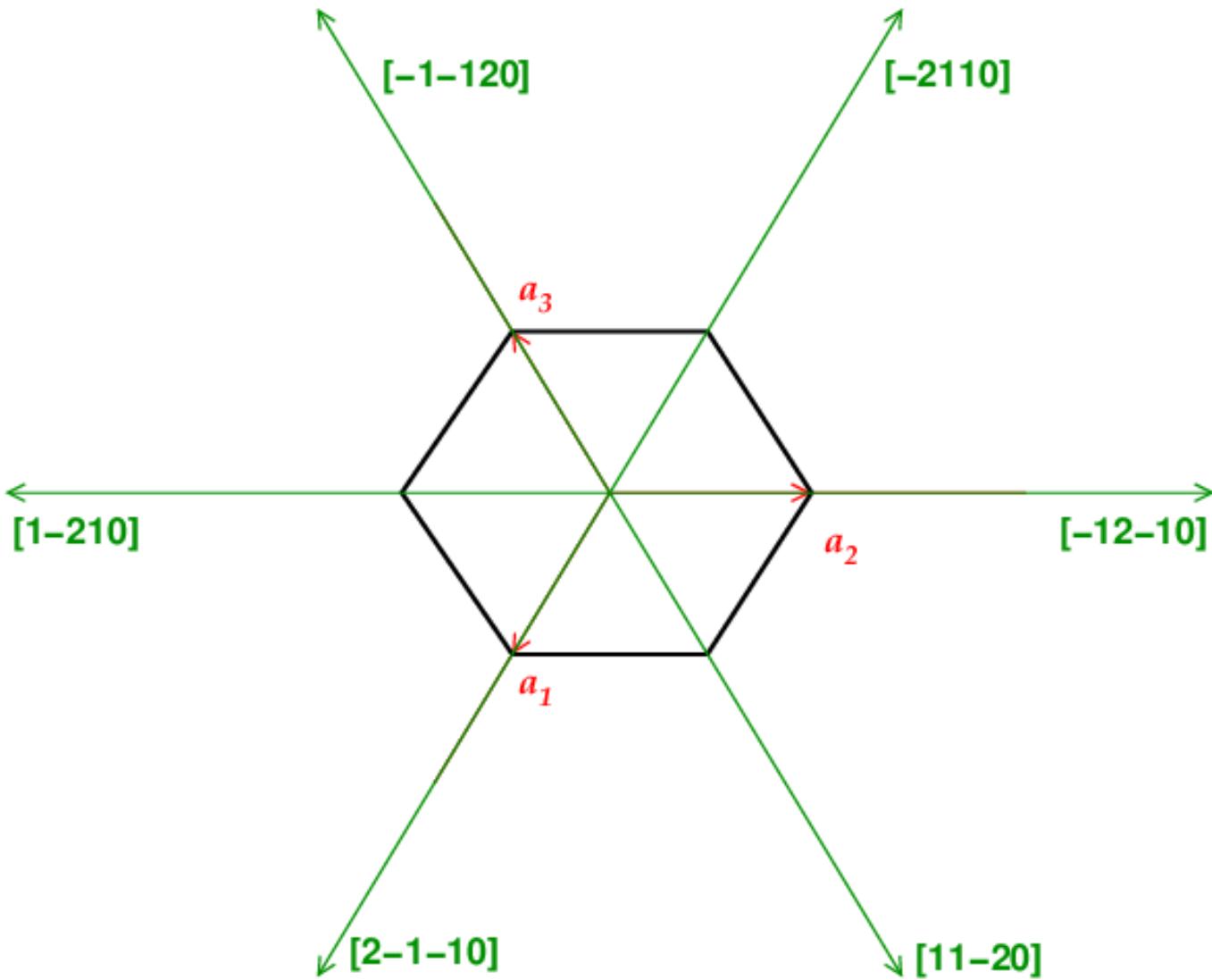
- Definition of Miller indices on 3 non-orthogonal axes (a_1 , a_2 et c): can be used but will hide symmetry operations
- Definition of Miller indices on 3 orthogonal axes (a_1 , a_2 et c) can be used but it is easy to use (loss of symmetry elements, difficult to correlate to the crystal structure).

Hence: 4 indices notation:

- For planes: $(hkil)$ avec $h+k+i=0$;
- h , k , and l are identical to those of the 3 indices notation
- For direction: conversion between 3 and 4 indices is more complex
 - $u = (2u'-v')/3$; $v = (2v'-u')/3$; $t = -(u+v)$
 - $w = w'$
 - $[uvtw]$ with $u+v+t=0$



Direction examples (1)

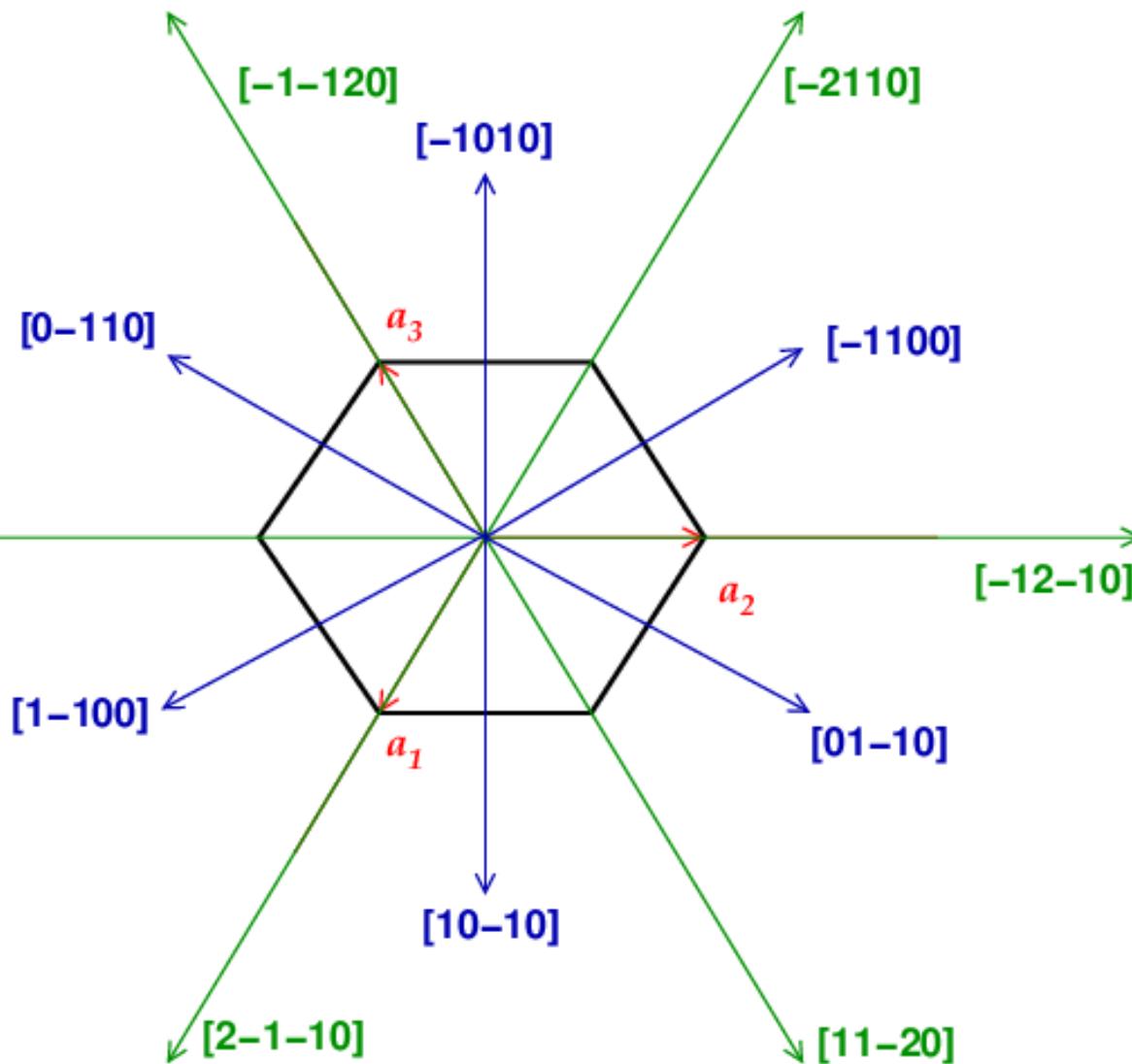


Practice:

Pot the $[2\bar{1}10]$ and
 $[11\bar{2}0]$ directions

All other
equivalents

Direction examples (2)



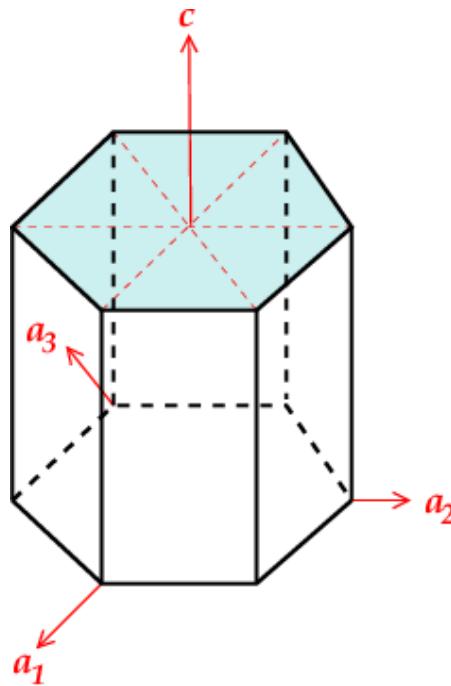
Practice:

Plot the $[10\bar{1}0]$ and $[01\bar{1}0]$ directions and all other equivalent directions.

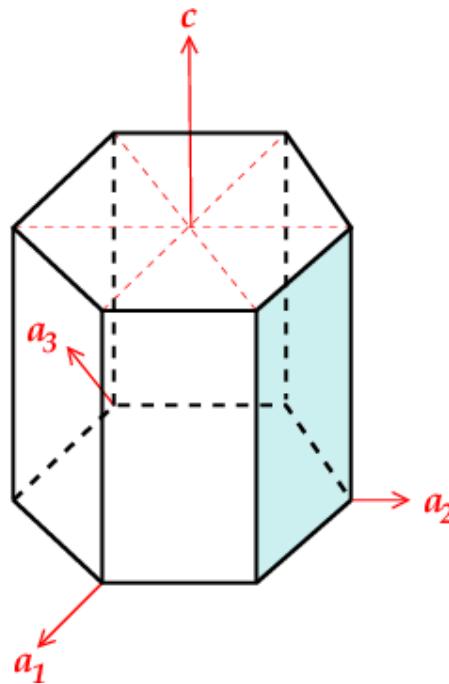
Also note

- For directions in the basal plane: $[hki0]$ is orthogonal to the $(hki0)$ plane.
- It is not true for $(hkil)$ planes if $l \neq 0$.

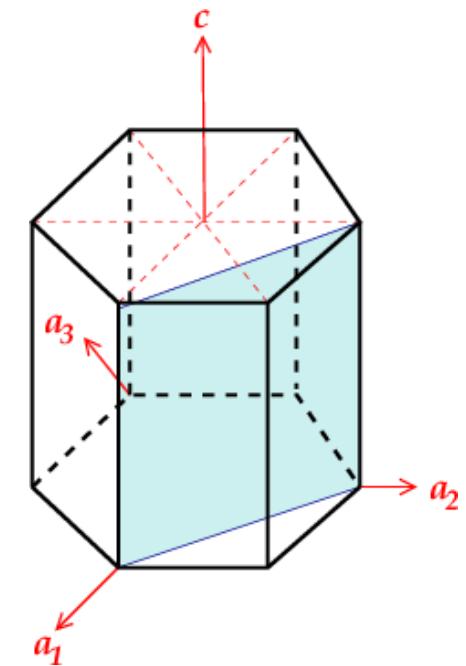
Basal and prismatic planes



(0001)
Basal plane
 $\{0001\} : (0001)$

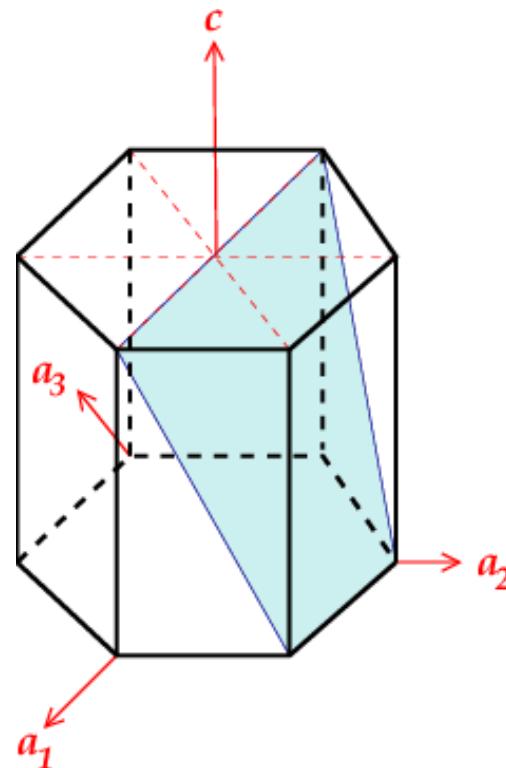


(01 $\bar{1}$ 0)
Prismatic plane
 $\{01\bar{1}0\} :$
 $(01\bar{1}0), (\bar{1}100), (\bar{1}010)$

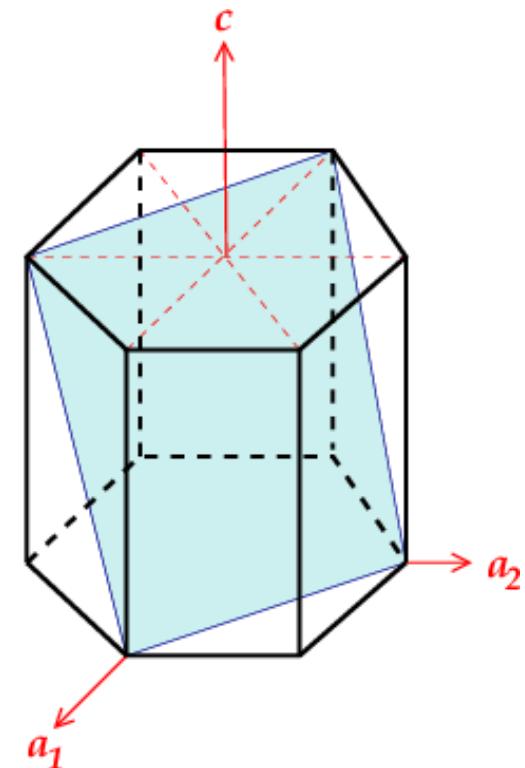


(11 $\bar{2}$ 0)
No name
 $\{11\bar{2}0\} :$
3 equivalents

Pyramidal planes

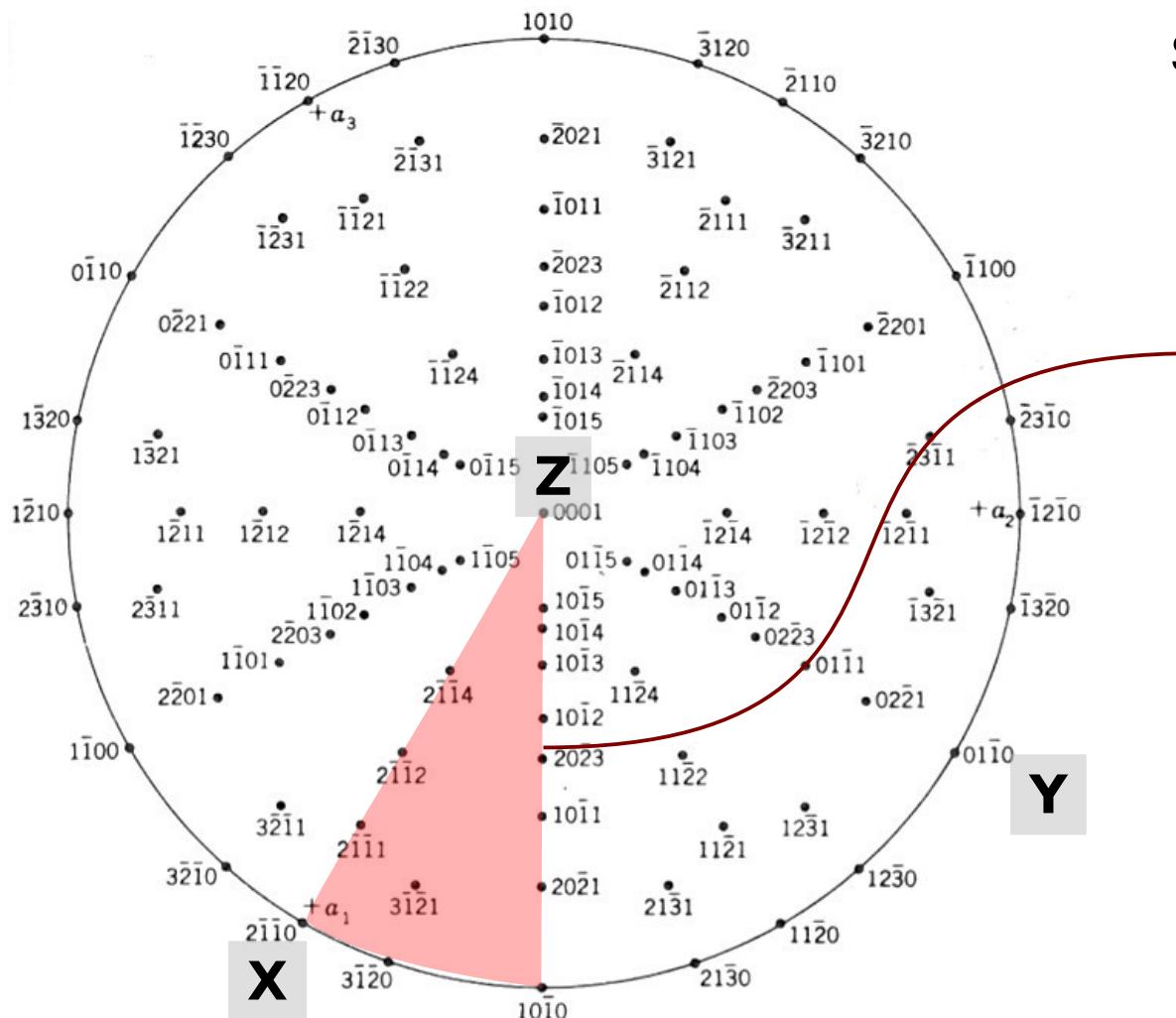


$(01\bar{1}1)$
Pyramidal plane
 $\{01\bar{1}1\}$:
6 equivalents



$(11\bar{2}1)$
Second order pyramidal plane
 $\{11\bar{2}1\}$:
6 equivalents

Stereographic projection



Stereographic projection for hcp-Zn

Hexagonal sector: sufficient for plotting inverse pole figures

Z // [0001], perpendicular to the basal plane

X // [2-1-10], parallel to a_1

Y // [01-10], perpendicular to a prismatic plane

Fig. 2-10 Standard (0001) projection for zinc (hexagonal, $c/a = 1.86$).

Barret & Massalski, Structure of Metals,
Permagon (1980)

c/a parameter

The *c/a* parameter is related to the compact nature of the structure

- True compact structure: $c/a = 1.633$
- The *c/a* parameter has a large influence on plastic deformation in hcp metals

$c/a > 1.633$

$c/a \sim 1.633$

$c/a < 1.633$

Métal		<i>c/a</i>
Cadmium	Cd	1,886
Zinc	Zn	1,856
Magnésium	Mg	1,623
Cobalt	Co	1,623
Rhénium	Re	1,615
Zirconium	Zr	1,592
Osmium	Os	1,589
Titane	Ti	1,587
Béryllium	Be	1,568